On the Notion of Functional Aspects in Aspect-Oriented Refactoring

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Abstract. In this paper, we examine the notion of functional aspects in context of aspect-oriented refactoring. Treating aspects as functions reduces the potential interactions between aspects significantly. We propose a simple mathematical model that incorporates fundamental properties of aspects and their interactions. Using this model, we show that with regard to refactoring functional aspects are as flexible as traditional aspects, but with reduced program complexity.

1 Introduction

Aspect-oriented refactoring (AOR) is the process of decomposing a legacy program into a well-structured core and a set of aspects that implement concerns that crosscut the core functionality. This process, also referred to horizontal decomposition \cite{9}, untangles the structure of a legacy program by gradually detaching code pieces and encapsulating them in aspects.

The essence of AOR can be formulated using simple mathematics. The following equation expresses the relation between a legacy program $P$ and a program $P'$ that was refactored in order to detach aspect $A$:

$$P = A \ast P'$$  \hspace{1cm} (1)

The operator `$\ast$' denotes aspect weaving. Aspects are detached in a step-wise manner. In its general form, AOR means decomposing program $P$ incrementally into an untangled core program $P'$ and $n$ aspects $A_i$:

$$P = A_1 \ast A_2 \ast \ldots \ast A_{n-1} \ast A_n \ast P'$$ \hspace{1cm} (2)

AOR can be understood as the inverse process of aspect weaving. While the former process detaches aspects of a program, the latter attaches aspects. While introductions of an aspect (as defined in AspectJ) are targeted to the classes of program $P'$, advice can have global effects. That is, an advice in aspect $A_i$ can advise an aspect $A_j$, for any pair $(i, j)$ (Fig. 1). In theory, the number of potential aspect interactions ($A_i$ advises or refers to $A_j$) grows by $O(n^2)$, although in practice, a desire is for aspect interactions be either well-understood or non-existent. Note, the refactoring order of aspects is not necessarily equivalent to aspect weaving order, especially if aspects are independent of each other.
AOR and step-wise development. A different perspective to understand aspects and AOR can be found in the practice of stepwise software development (SWD) [7, 8, 3, 2]. The idea behind SWD is to develop a program from a minimal base and successively applying refinements that implement different design decisions, called development steps.

Usually, refinements in SWD are modeled as functions; they take a program as input and produce a modified program as output. This interpretation is not far from the intuitive understanding of aspects. For example, aspect $A$ takes program $P'$ as input and produces the modified program $P$:

$$ P = A(P') $$

A sequence of $n$ factored aspects is modeled by function composition, where function application is (a form of) aspect weaving:

$$ P = A_1(A_2(\ldots A_{n-1}(A_n(P'))\ldots)) $$

This sequence could be continued by substituting $P'$ for a detached aspect $A_{n+1}$ that takes a refactored program $P''$ as input.

At the first glance, the notion of functional aspects seems to be only a mathematical or even notational concern. But there are some deeper issues, as we will explain: Notably, SWD and function composition impose a fixed order on weaving. This is because of refinements affect and extend only that program that was produced by previous development steps [7]. This restriction limits the number of potential interactions between different refinements and therewith improves program comprehensibility. As Figure 2 shows, modeling aspects as functions leads to a different interaction pattern, one that is theoretically half as complex compared to the traditional one, shown on Figure 1. As intended for traditional aspects, it is desired for the interactions of functional aspects to be either well-understood or non-existent.

With functional aspects, the weaving order is unidirectional; aspects affect only aspects that were woven previously. This enables us to define the refactoring order as the inverse to the weaving order. This definition is valid since all aspects $A_i$ may only affect subsequently detached aspects $A_j$ with $j > i$.

Aspect quantification. The differing interaction patterns result from different interpretations of aspect quantification. While traditional aspects are quantified globally, functional aspects are quantified locally (they affect only previously woven aspects). This results in a fundamental difference between SWD and AOP.
Nevertheless, functional aspects have the strength that the number of possible interactions is half of the number of the traditional approach. Their underlying model has the potential for formalizing the effects of aspects that is in line with prior research on software design and program generation [8, 7, 3, 2, 1, 5]. In this paper, we examine functional aspects in the light of AOR. As mentioned, the unidirectionality of functions imposes a fixed weaving order, but also a fixed refactoring order. That is, we cannot factor out an aspect $A$ and subsequently factor out aspect $B$ with $B$ affecting $A$. This is not allowed with functional aspects. Given these facts, it would seem that refactoring functional aspects would be more difficult than refactoring traditional aspects, because the order in which aspects are composed must known a priori. That is, it would seem that $A_1$ must be refactored first in (4), then $A_2$, ... and finally $A_n$. Knowing this order up-front seems unlikely.

**Perspective, goals, and contributions.** We believe that the concept of functional aspects matches very closely with prior work in software design and automated software development. Their main benefit is that the number of potential aspect interactions is half of the one of traditional aspects. A fundamental question regarding functional aspects is: does the order in which functional aspects are refactored matter? And can mathematical models of the effects that functional aspects make to a program provide help in answering this question?

In this paper, we explore answers to these questions. Our analysis allows us to demonstrate a flexibility in refactoring functional aspects that is normally attributed to traditional aspects, i.e., that the order in which traditional aspects are refactored does not matter. (Note: that we believe that the refactoring-aspects-order-does-not-matter is an assumption of the AOP community; our results may suggest why this assumption has a basis in fact). We demonstrate how a mathematical model may help to promote refactoring approaches, in particular, we show how to transform functional (and also traditional) aspects in a way that they become commutative with respect to the refactoring order.

## 2 Aspect Interactions and Dependencies

In our analysis we focus on the following kinds of interactions:

**References.** Aspects that refer to other aspects depend on these aspects. Such referential dependencies are for example method calls or advising other aspects. Treating aspects as functions implies that referred aspects have to be woven before the referring aspects; as mentioned, with traditional aspects the order does not matter.

**Overlapping join points.** Aspects interfere with other aspects when advising the same join point. In case of overlapping join point sets, the order of aspects matters, because different orders result in different program semantics. The right order has to be inferred from the domain, i.e. which aspect advises a join point first. With respect to overlapping join point sets, both kinds of aspects behave equally.
3 Algebraic Properties

Dependencies between functional aspects impose a fixed refactoring order. In this section, we show how to alter this order without affecting the program semantics. On one hand, this demonstrates similar flexibility with traditional aspect semantics. On the other hand, it gives evidence that the refactoring order does not matter.

Altering the order of refactoring is achieved by respectively swapping two aspects, or more precisely swapping the composition order. Functional aspects can be swapped if they are commutative. Otherwise, we exploit a notion which we call pseudo-commutativity to create swappable aspects.

3.1 Commutativity

Two aspects $A$ and $B$ are commutative if they can be swapped, and this does not affect the program semantics. Commutativity is the ideal case and yields the most flexibility in permuting the refactoring order.

$$A(B(P)) = B(A(P)) \tag{5}$$

The left-hand side of the equality means $A$ is factored first, then $B$; the right-hand side means $B$ is factored first, and then $A$.

A precondition for commutativity of aspects is that these aspects do not depend on each other – this means there are no referential dependencies and no join point overlapping. Figure 3 lists two aspects $Foo$ and $Bar$ that are commutative with respect to a program. They do not refer to each other and they advise a disjoint set of join points (calling $m$ and $n$).

```
1 aspect Foo {
2   before() : call(* n()) { ... }
3 }
4 aspect Bar {
5   before() : call(* m()) { ... }
6 }
```

Fig. 3. Two commutative aspects.

3.2 Pseudo-Commutativity

Two aspects $A$ and $B$ are pseudo-commutative (1) if they are not commutative, but (2) they can be transformed to $A'$ and $B'$ so that swapping them does not affect the program semantics.

$$A(B(P)) = B'(A'(P)) \tag{6}$$

The above equation means that for each pseudo-commutative pair $A$ and $B$ there is at least one pair $A'$ and $B'$ that, when swapped, does not change the program semantics.

\footnote{For simplicity, we depict both aspects in the same listing. The order in the listing is arbitrary and does not refer to any order.}
semantics. Hence, a programmer may implement aspects with this property in several ways, e.g. A or instead A'. If functional aspects are pseudo-commutative, the order of refactoring does not matter. The programmer can always find for each aspect an appropriate implementation that fits the already factored sequence of aspects. In our example, it does not matter if we factor A first and then B, or B' first and then A'. Although the implementations of A and B differ from A' and B', they implement the same concerns, but in a different way.4

In the following, we illustrate several examples of pseudo-commutativity.

**Resolving referential dependencies.** Let Foo and Bar be aspects, and Foo refers to Bar by calling the static method bar (Fig. 4). Since we treat aspects as functions, Bar has to be woven first because of the referential dependency; the only correct order is Foo(Bar(Prog)).

![Fig. 4. Two referential dependent aspects.](image)

However, applying the notion of pseudo-commutativity, we are able to derive Foo' and Bar' so that the expression Bar'(Foo'(Prog)) equals Foo(Bar(Prog)). By doing this, we achieve the same flexibility as traditional aspects. Figure 5 depicts one possible pair of Foo' and Bar'.

![Fig. 5. Resolving referential dependencies.](image)

Foo' no longer refers to Bar' (Line 2), i.e. Foo' does not directly call method bar. In order not to affect the program behavior, Bar' itself triggers the call of bar by introducing an advice (Lines 8-9). The advice is executed before that join point in Foo' that is responsible for calling bar. Note that the basic meaning or effect of Foo and Bar (advising n and m as well as bar is invoked when is foo is executed) is preserved by Foo' and Bar'.

In the above example, we removed a method call to another aspect in order to swap both. Now suppose that one aspect refers to another by means of an advice. Interestingly, this is exactly the opposite case of removing a method call

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4 A related idea can be found in design maintenance systems: Program transformations implement design decision in stepwise manner. Baxter has shown that the order of design decisions can be altered by altering the transformations [4].
reference. Take Bar’ and Foo’ as example (Fig. 5): Bar’ advises Foo’. To remove this reference (in order to swap them), we have to find their pseudo-commutative counterparts – these are exactly the original aspects Foo and Bar (Fig. 4).

**Cyclic referential dependencies.** Cyclic referential dependencies are a special case of referential dependencies. Figure 6 shows that aspect Foo refers to Bar by advising bar (Line 3); the advice invokes method adviceBar. Symetrically, Bar refers to Foo by advising foo (Line 7). If we cannot remove such cyclic referential dependencies, we have an example where traditional aspects are more flexible. This is because with traditional aspect semantics, the following two composition orders would be correct: Foo ∗ Bar ∗ Prog and Bar ∗ Foo ∗ Prog.

```
1 aspect Foo {
2   void foo () { ... }
3   before() : execution(void Bar.bar()) { adviceBar(); }
4 }
5 aspect Bar {
6   void bar () { ... }
7   before() : execution(void Foo.foo()) { adviceFoo(); }
8 }
```

**Fig. 6.** Cyclic referential dependencies.

To remove cyclic referential dependencies the idea of sandwiching helps [7]. Although sandwiching is a mechanism to resolve cyclic dependencies in uses-hierarchies, it can be adopted to our problem. Using sandwiching, we can split each pair of cyclic referential dependent aspects A and B into A₁, A₂ and B₁ and B₂ so that:

\[
A_2 (B_2 (A_1 (B_1 (P)))) = B_2 (A_2 (B_1 (A_1 (P)))) \tag{7}
\]

A₂ refers to B₁ and B₂ to A₁. This is called sandwiching because of A₂ and A₁ embrace B₂, and B₂ and B₁ embrace A₁. After this transformation the ordering of (B₁, A₁) and (B₂, A₂) can be swapped pairwise. Since we eliminated cycles, the remaining referential dependencies can be removed for further swapping, i.e. (B₁, B₂) and (A₁, A₂).

Figure 7 illustrates the sandwiching of the aspects Foo and Bar (cf. Fig. 6):

\[
\text{Foo}(\text{Bar}(\text{Foo}(\text{Bar}(\text{Prog})))) = \text{Bar}(\text{Foo}(\text{Bar}(\text{Foo}(\text{Prog})))) \tag{8}
\]

Foo₁ defines method foo (Line 10); Bar₁ defines method bar (Line 13); Foo₂ and Bar₂ encapsulate the dependent code. But now Foo₂ refers to Bar₁ (Lines 2-3), and Bar₂ to Foo₁ (Lines 6-7). Hence, Foo₂ and Bar₂ can be swapped since they only depend on Foo₁ and Bar₁. Since Foo₁ and Bar₁ do not depend on one another, they can be swapped as well.

However, sandwiching is only the first step to derive the two possible orderings mentioned above: Foo(Bar(Prog)) and Bar(Foo(Prog)). But now that there are only unidirectional referential dependencies left, we can further transform the aspects by exploiting pseudo-commutativity in order to permute their
ordering; we can derive the orderings $\text{Bar}^2(\text{Bar}^1(\text{Foo}^2(\text{Foo}^1(\text{Prog}))))$ (Fig. 8) and $\text{Foo}^2(\text{Foo}^1(\text{Bar}^2(\text{Bar}^1(\text{Prog}))))$ (Fig. 9), whereby respectively the parts of $\text{Bar}$ can be merged again, and symmetrically the parts of $\text{Foo}$. After this step, we are able to derive both orders $\text{Bar}(\text{Foo}(\text{Prog}))$ and $\text{Foo}(\text{Bar}(\text{Prog}))$, as with traditional aspects.

**Fig. 7.** Sandwiching for resolving cyclic dependencies.

**Fig. 8.** Ordering: $\text{Bar}^2(\text{Bar}^1(\text{Foo}^2(\text{Foo}^1(\text{Prog}))))$.

**Fig. 9.** Ordering: $\text{Foo}^2(\text{Foo}^1(\text{Bar}^2(\text{Bar}^1(\text{Prog}))))$.

Resolving join point overlapping. Two aspects interact with each other if they advise overlapping sets of join points. Naturally, the order matters in this situation, for functional and traditional aspects. Weaving in different orders results in different execution orders of the connected advice. Suppose $\text{Foo}$ and $\text{Bar}$ advise the same method call (Fig. 10); both aspects were already factored out. Changing the refactoring and thereby the following weaving order would result in semantically differing programs because either $\text{foo}$ is called before $\text{bar}$ or vice versa. However, with AspectJ it is possible to define a weaving order explicitly, but this can be complicated and not all desired orders can be expressed [5].

We use pseudo-commutativity to resolve join point overlapping. This methodology is useful for both kinds of aspects. Suppose method $n$ is called in a main
method (Fig. 11). Right before calling method \texttt{n} our two concerns (later on implemented by \texttt{Foo} and \texttt{Bar}) are to be executed. Factoring both concerns using the above depicted aspects would be possible only in one order, first \texttt{Bar} then \texttt{Foo}. In order to be able to swap \texttt{Foo} and \texttt{Bar}, we can prepare the code associated with the target join points themselves. We simply add hooks for each advice that is supposed to bind to the join points. The methodology of preparing code is in line with the observation of Murphy et al. [6].

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{chart1.png}
\caption{Join point overlapping.}
\end{figure}

![Fig. 10. Join point overlapping.](chart1.png)

Figure 12 shows the refactored \texttt{main} function. The both hooks \texttt{hookFoo} and \texttt{hookBar} implement the corresponding concern functionality. Then, when refactoring out \texttt{Foo} and \texttt{Bar} as aspects the (empty) hook methods mark their join points. The hooks fix the concern execution order. They enable us to alter the refactoring order (first \texttt{Foo}, then \texttt{Bar}) because now we bind the aspects not to calling \texttt{n}, but to calling the hooks (Fig. 13). Thus, the order of refactoring no longer influences the order of execution, with functional aspects and traditional aspects.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{chart2.png}
\caption{A target join point for \texttt{Foo} and \texttt{Bar}.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{chart3.png}
\caption{Binding advice to hooks.}
\end{figure}

\section{Conclusions}

In this paper we examined the flexibility of functional aspects in context of AOR. We presented a simple algebraic approach that models aspects as functions. This is in line with prior work on software design and composition. We explored if functional aspects are as flexible as traditional aspects with respect to altering
the refactoring order. We raised this question because, on one hand, treating aspects as functions reduces program complexity by decreasing the number of potential aspect interactions, and, on the other hand, it seemed that the traditional model was more flexible w.r.t. the ordering of aspects. In order to address these issues, we analyzed the properties and dependencies of functional aspects. We used our mathematical model to abstract over implementation details and to be able to make general statements.

Specifically, we have shown that certain kinds of aspect dependencies caused by references and overlapping join points can be resolved by applying the notion of pseudo-commutativity. Both kinds of aspects are similarly flexible with respect to the order of refactoring. We claim that each pair of aspects with referential dependencies or overlapping join points can be transformed into a corresponding pseudo-commutative pair. While our ideas are preliminary, we believe our theory offers practice potential in future AOR technologies.

With this study we could show that the SWD perspective does not constrain the known techniques of AOR. It has the same power than the traditional approach but reduces potential interactions. It is more disciplined and advantageous with regard to complexity and comprehensibility [5].

Our next task is to decompose larger applications to test the validity of our ideas. This is a subject of on-going work.

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